

8-7: Composition of Functions 1

On a vacation to Europe you need to convert your U.S. American Dollars to Irish punts.

However, we only know that the formula to convert British pounds to Irish punts

$$B(x) = 0.9733x$$

American Dollars to British pounds

$$A(x) = 0.6252x$$

How do we find a direct equation to convert American Dollars to Irish punts?

$$B[A(x)] = 0.9733x$$

↑
0.6252x

$$B[A(x)] = 0.9733(0.6252x)$$

$$B[A(x)] = 0.6085x$$

This converts American to Irish
\$ 500 \rightarrow 304.25 Irish punts

Basically, plugging one function
into another is called
a composition of functions.

Example: If $f(x) = x^2 - 4$
and $g(x) = 4x - 1$

Find $[f \circ g](x)$.

This is read as
"F of g of x."

also written as $F[g(x)]$

$$\begin{aligned}
 & x^2 - 4 \\
 & \downarrow \\
 & (4x - 1)^2 - 4 \\
 & (4x - 1)(4x - 1) - 4 \\
 & 16x^2 - 8x + 1 - 4
 \end{aligned}$$

$$F[g(x)] = 16x^2 - 8x - 3$$

Find $[g \circ f](x) = G[f(x)]$

$$\begin{aligned}
 G &= 4x - 1 \\
 &= 4(x^2 - 4) - 1
 \end{aligned}$$

plug in $f(x)$

$$4x^2 - 16 - 1$$

$$G[f(x)] = 4x^2 - 17$$

Example $f(x) = x + 5$ $g(x) = x^2 - 2$

Find $[f \circ g](3) \rightarrow F[g(3)]$

$$\begin{array}{c} x + 5 \\ \downarrow \\ (x^2 - 2) + 5 \end{array}$$

$$3^2 - 2 + 5$$

$$9 - 2 + 5 = \boxed{12} \text{ Yahoo!}$$

Find $G[f(3)]$

$$G = x^2 - 2$$

$$G[f(3)] = (x + 5)^2 - 2$$

$$= (3 + 5)^2 - 2$$

$$= 8^2 - 2$$

$$= 64 - 2 = \boxed{62}$$

Assignment :

$$F(x) = x + 6$$

$$G(x) = x - 3$$

$$F[G(2)] \quad \& \quad G[F(2)]$$

$$x + 6$$

$$x - 3$$

$$(x - 3) + 6$$

$$(x + 6) - 3$$

$$2 - 3 + 6$$

$$(2 + 6) - 3$$

$$(5)$$

$$(5)$$