

Sec 10-2: Logarithms

Logarithms (Logs) are exponents.

Logarithms were most useful before computers, to simplify calculations using a base raised to an exponent.

The system works like this:

Exponential Equation

$$b = n$$

Annotations: "exponent" with an arrow pointing to p ; "base" with an arrow pointing to b ; "the number (answer)" with an arrow pointing to n .

Logarithmic Equation

$$\log_b n = p$$

Annotations: "base" with an arrow pointing to b ; "#" with an arrow pointing to n ; "exponent" with an arrow pointing to p .

Ex.) $2^5 = 32$

* $\log_2 32 = 5$

* This is read as "the \log base 2 of 32 is equal to 5."
 (An arrow points from the word "log" to the text "refers to the exponent.")

More examples

Exponential Equation

$$5^2 = 25$$

$$10^5 = 100,000$$

$$8^0 = 1$$

$$2^{-4} = \frac{1}{16}$$

$$9^{\frac{1}{2}} = 3$$

Log Equation

$$\log_5 25 = 2$$

$$\log_{10} 100,000 = 5$$

$$\log_8 1 = 0$$

$$\log_2 \frac{1}{16} = -4$$

$$\log_9 3 = \frac{1}{2}$$

Complete

* log base must be > 0
and $\neq 1$. "The number", n ,
must also be > 0 .

ex.) write $2^5 = 32$ in log form: $\log_2 32 = 5$

ex.) write $\log_5 125 = 3$ in exponential: $5^3 = 125$

Solve

$$\log_9 X = \frac{3}{2}$$

$$9^{\frac{3}{2}} = X$$

$$\sqrt[2]{9^3} = X$$

$$27 = X$$

Evaluate

$$\log_3 \frac{1}{27}$$

$$\log_3 \frac{1}{27} = X$$

$$3^X = \frac{1}{27}$$

$$3^{-3} = \frac{1}{27}$$

$$X = -3$$

Solve

$$\log_4 256 = y$$

$$4^y = 256$$

$$y = 4$$

Evaluate

$$\log_{16} 4 = X$$

$$16^X = 4$$

$$(4^2)^X = 4^1$$

$$\frac{2X}{2} = \frac{1}{2}$$

$$X = \frac{1}{2}$$